

# Progressive failure on the North Anatolian fault since 1939 by earthquake stress triggering

Ross S. Stein,<sup>1</sup> Aykut A. Barka<sup>2</sup> and James H. Dieterich<sup>1</sup>

<sup>1</sup>US Geological Survey, MS 977, Menlo Park, CA 94025 USA. E-mail: rstein@usgs.gov; jdieterich@usgs.gov

<sup>2</sup>Istanbul Technical University, Department of Geology, Istanbul, 80626 Turkey. E-mail: barka@sariyer.cc.itu.edu.tr

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## SUMMARY

10  $M \geq 6.7$  earthquakes ruptured 1000 km of the North Anatolian fault (Turkey) during 1939–1992, providing an unsurpassed opportunity to study how one large shock sets up the next. We use the mapped surface slip and fault geometry to infer the transfer of stress throughout the sequence. Calculations of the change in Coulomb failure stress reveal that nine out of 10 ruptures were brought closer to failure by the preceding shocks, typically by 1–10 bar, equivalent to 3–30 years of secular stressing. We translate the calculated stress changes into earthquake probability gains using an earthquake-nucleation constitutive relation, which includes both permanent and transient effects of the sudden stress changes. The transient effects of the stress changes dominate during the mean 10 yr period between triggering and subsequent rupturing shocks in the Anatolia sequence. The stress changes result in an average three-fold gain in the net earthquake probability during the decade after each event. Stress is calculated to be high today at several isolated sites along the fault. During the next 30 years, we estimate a 15 per cent probability of a  $M \geq 6.7$  earthquake east of the major eastern centre of Ercinzan, and a 12 per cent probability for a large event south of the major western port city of Izmit. Such stress-based probability calculations may thus be useful to assess and update earthquake hazards elsewhere.

**Key words:** earthquake prediction, seismic modelling, seismic stress, stress distribution.

## INTRODUCTION

Like falling dominoes, four westward-migrating earthquakes ruptured 725 km of the North Anatolian fault during 1939–1944, with subsequent earthquakes extending the zone of faulting eastwards and westwards (Fig. 1). This classic case of progressive earthquake failure has tantalized earth scientists (Richter 1958; Allen 1969; Dewey 1976; Jackson & McKenzie 1988; Scholz 1990), and terrorized insurance providers, for half a century. Although clustering of earthquakes in space and time is common (Dieterich 1994; Kagan & Jackson 1991), and migrating earthquake sequences have occurred elsewhere (Kasahara 1981; Mogi 1985), none is as spectacular as on the North Anatolian fault. Most recently, Roth (1988) modelled the shear stress build-up along the western part of the North Anatolian fault using a simple fault geometry with collinear ruptures of uniform slip, and found that the stress at future ruptures was generally raised by the preceding events.

New observations of the North Anatolian fault, as well as new methods to calculate how seismic stress transfer alters the probability of subsequent earthquakes, encourage us to revisit this sequence to learn what conditions promote progressive

failure. Until recently, the fault geometry was poorly known, and there were few measurements of the 1939–1944 earthquake fault slip (Ketin 1969; Ambraseys 1970), precluding calculation of the earthquake-induced stresses. Nor could the stress transferred by the steady or ‘secular’ stress accumulation be calculated, since the rate of deep fault slip driving the stress build-up was uncertain by a factor of 4 (Jackson & McKenzie 1988; Barka 1992; Le Pichon *et al.* 1993). New findings remove these obstacles: a three-fold increase in measurements of earthquake slip, including a twelve-fold increase for the largest 1939 shock (Barka 1996), provides data essential to model the earthquake stress changes (Fig. 1b). New detailed fault mapping (Barka 1992; Saroglu & Kusçu 1992) (Fig. 1c) reduces the uncertainty in the fault location from about  $\pm 25$  km to  $\pm 5$  km. Finally, geodetic analyses yield the slip rate along the fault (Oral 1994; Straub & Kahle 1994; Straub 1996).

The North Anatolian fault emerges as a close analogue of the San Andreas fault in California, with the two continental transforms sharing similar slip rates, total length, and straightness relative to their poles of rotation (Fig. 1a). But while the San Andreas fault produced just two  $M \geq 6.7$  earthquakes in this century (in 1906 and 1989), the North Anatolian fault has

suffered 10 such shocks, thus providing a superior natural laboratory to study earthquake interaction (Figs 1b and c). Ruptures from Parkfield to the Salton Sea within 5 yr would, for example, be a comparable sequence on the San Andreas fault. We find that all but one earthquake increased the stress towards failure at the site of the subsequent shocks, and inhibited failure on most fault segments that did not rupture. We argue that the calculated several-bar stress increases raised the earthquake probability three-fold during the ensuing decade, and we suggest why migrating earthquake sequences are prevalent on the North Anatolian fault. Bolstered by recent findings that aftershocks and background seismicity concentrate where the stress has risen (Harris & Simpson 1992; Harris, Simpson & Reasenberg 1995; Jaumé & Sykes 1992; King, Stein & Lin 1994; Stein, King & Lin 1994; Jaumé & Sykes 1996), these results offer a new approach to updatable forecasts of earthquake hazard.

### COULOMB FAILURE STRESS CHANGE

We calculate the static Coulomb stress changes resulting from North Anatolian ruptures since 1939, with stress calculated in an elastic half-space at all points (as shown in Figs 3b, 4 and 5) or resolved on the fault plane (as listed in the tables and shown in Fig. 3a). Since we lack hypocentral depths for the Anatolian main shocks, we sample stress in the central part of the seismogenic crust at a depth of 8 km. Failure is facilitated on a plane when the Coulomb failure stress  $\sigma_f$  rises,

$$\sigma_f = \tau_\beta - \mu\sigma'_\beta, \quad (1)$$

where  $\tau_\beta$  is the shear stress on the failure plane  $\beta$  (positive in the direction of fault slip) and  $\sigma'_\beta$  is the effective normal stress (positive in compression);  $\mu\sigma'_\beta \approx \mu'\sigma_\beta$ , where  $\mu'$  is the apparent coefficient of friction with range 0.0–0.75. The confining stress can be related to fluid pore pressure by Skempton's coefficient,  $B$ , the ratio of the change in pore pressure in a cavity to the change in applied stress, where  $\mu' = \mu(1 - B)$  (Roeloffs 1988). Immediately after the earthquake,  $B \approx 2/3$ , but could fall to zero if fluids were to drain fully from the fault zone (Scholz 1990). We set  $\mu' = 0.4$ , equivalent to laboratory values of friction ( $\mu \sim 0.75$ ) and moderate pore pressure if fluids are not fully expelled ( $B \sim 0.5$ ), or to a low value of friction as inferred for the San Andreas fault (Zoback *et al.* 1987). A  $\mu'$  of 0.4 also minimizes the calculation error caused by the uncertainty in  $\mu'$  to  $\pm 25$  per cent (King, Stein & Lin 1994); compare, for example, column 2 (for  $\mu' = 0.75$ ) and column 3 (for  $\mu' = 0.40$ ) in Table 2.

### Secular stress change

In addition to earthquakes, steady slip beneath the North Anatolian fault system transfers stress to the seismogenic portion of the fault. This we model with slip tapering from 0 at 12.5 km depth to the full rate below 24 km (Fig. 2a). GPS data give  $24 \pm 4$  mm yr<sup>-1</sup> along the North Anatolian fault (Oral 1994); near its western end, slip is partitioned with 16 mm yr<sup>-1</sup> along the Karamürsel–Sapanca faults and 9 mm yr<sup>-1</sup> along the Iznik–Geyve faults (Straub & Kahle 1994; Straub 1996). GPS data also resolve left-lateral slip of  $18 \pm 6$  mm yr<sup>-1</sup> on the East Anatolian fault and  $\sim 5$  mm yr<sup>-1</sup> on the Northeast Anatolian fault (Bennett, Reilinger & Barka, in preparation; Oral 1994) (Figs 1c and 2). During a complete

earthquake cycle in this model, coseismic slip would take place over 0–12.5 km and secular slip over 12.5–100 km. Such a model will not produce uniform stress even when averaged over many earthquake cycles, since the fault strike and coseismic slip are both variable (Fig. 1b). In addition, we neglect postseismic slip beneath 12.5 km, so we probably underestimate the total stress transfer during the cycle.

Shear stress builds in this model at 0.15 bar yr<sup>-1</sup> along most of the North Anatolian fault (Fig. 2b). Because uniform right-lateral slip is imposed beneath a relatively straight North Anatolian fault at depth, appreciable normal stress is transferred to the fault at seismogenic depths only at fault bends (such as at km -350 to -400, or km 500–550). A uniform stress increase of 0.01 bar yr<sup>-1</sup> is added at all points to account for the small residual stressing on faults more than 100 km from the Anatolian fault system (Fig. 1a). This small addition of stress keeps the secular stress build-up positive at all sites in the model.

### Resolved and optimally oriented stress changes

The Coulomb stress change caused by the 1939 earthquake is resolved on major faults in Fig. 3(a). Shear and normal stress is resolved on the fault surface (projected in UTM coordinates) at a depth of 8 km. Faults are assumed to be vertical and to slip in the sense indicated by the arrows, except for the west end of the 1939 rupture, which dips 50°N and has oblique reverse slip. The apparent coefficient of friction,  $\mu'$ , is assumed to be 0.4; no information about the regional stress is needed for this calculation. The Coulomb stress is seen to drop by 50–100 bars along most of the 1939 rupture, with increases of several bars along the west end, beyond the east end, and along most of the succeeding 1942 fault rupture zone. The resolved stress changes are sensitive both to position and fault strike. Note that a right-lateral Coulomb stress of 100 bars is not equivalent to a left-lateral Coulomb stress of -100 bars on the same fault unless  $\mu' = 0$ , because, unlike the shear stress change, the sign of the normal stress change is the same for right- and left-lateral slip (e.g. fault-normal tension always favours failure). Thus the resolved stresses depend on inferring the sense of slip on each fault correctly. This result for the 1939 rupture, and for all succeeding events, is summarized in Tables 1–4.

The Coulomb stress change on optimally oriented vertical strike-slip faults (King *et al.* 1994) is plotted in Fig. 3(b) at a depth of 8 km. To create such a map, one must impose an orientation, and to a lesser extent, magnitude, of the regional (or tectonic) stress,  $\sigma^f$ . Here we assume a 100-bar uniaxial compression oriented 55° clockwise from the fault as shown by the white opposed arrows in Figs 2(b) and 4(a). About a dozen sites along the North Anatolian fault exhibit geological indicators of the orientation of the principal compression axis (Suzanne *et al.* 1990; Andrieux *et al.* 1995; Neugebauer 1995); they average 58° relative to the local strike of the North Anatolian fault. The principal strain-rate axes (Oral 1994) measured geodetically from the Marmara Sea to the central 1939 rupture zone indicated an axis oriented 48° clockwise from the fault. We use a weighted average of these observations. Dynamic models (Gülen, Barka & Toksöz 1987; Kasapoglu & Toksöz 1983), which consider the stresses imparted to the North Anatolian fault by remote plate tractions, yield a similar orientation.

Table 1. Earthquake parameters and stress transfer.

Earthquake Year	Moment Date	M <sub>0</sub> ** mag. M	M <sub>0</sub> ** (10 <sup>26</sup> dyn-cm)	Mean $\Delta\tau^*$ (bar)	Stress trigger <sup>‡</sup> (bar)	Trigger ratio <sup>§</sup> (%)	Time advance (yr) <sup>¶</sup>
1939	26 Dec	7.9	52.0	60	--	--	--
1942	20 Dec	6.9	1.7	42	4.7	11	8.4
1943	26 Nov	7.7	29.0	48	0.6	1	0.0
1944	01 Feb	7.5	15.0	34	5.8	17	31.4
1949	17 Aug	7.1	3.5	40	1.3	3	2.1
1951	13 Aug	6.8	1.4	25	1.7	7	11.0
1957	26 May	6.8	1.4	22	5.4	25	28.6
1966	19 Aug	6.6	0.6	15	8.2	55	30.0
1967	22 Jul	7.0	2.7	18	4.4	24	12.3
1971	22 May	6.8	1.2	11	3.5	32	4.6
1992	13 Mar	6.5	0.4	27	16.0	59	125.0
Average (all values)				31	5.2	24	25.3
Average (min/max excluded)				34	4.4	22	18.1

\*\* Seismic moment calculated from surface slip (Fig. 1), assuming a 0 to 12.5 km width of faulting, and a shear modulus  $G$  of  $3.15 \times 10^{11}$  dyne cm<sup>-1</sup>.

\* Mean static shear stress drop of all 5 km long rupture patches.

‡ Mean earthquake-induced plus secular stress change along future ruptures.

§ Stress trigger (col. 6) divided by succeeding earthquake stress drop (col. 5).

¶ Mean earthquake-induced stress change (for  $\mu = 0.4$ ) along the future rupture zone divided by the modelled secular stressing rate along that rupture.

The table shows three modes to assess the effect of the stress changes at the sites of future earthquakes. The trigger ratio is the Coulomb stress increase divided by the subsequent earthquake stress drop (col. 6/col. 5); the time advance gives the Coulomb stress increase divided by the local secular stressing rate.

The principal stresses are calculated from the tensor addition of the 100-bar regional stress, the earthquake stress change, and the secular stress, at every calculation point. Optimal planes are then calculated relative to the local principal stress axes. The internal angle between the right and left planes is a function of the apparent friction coefficient; the planes are orthogonal for  $\mu' = 0$ . Once the optimal planes are obtained, the earthquake plus secular stress changes are resolved on them. We thus calculate the change in Coulomb stress on planes that are optimally oriented after the earthquake. At any given point, the Coulomb stress changes along the optimum

right- and left-lateral planes are the same (the black and gray planes, respectively, in Figs 2b and 3b).

The earthquake stress change causes the optimum planes to rotate from the orientation imposed by the regional stress. In the limiting case that the regional stress is zero, all stress changes are positive and large rotations occur far from the source, regardless of whether such slip directions are possible in that environment. For an infinitely large regional stress, no rotations of the optimal planes occur, and the areas of the positive and negative fields exactly balance. For realistic assumptions about the regional stress (e.g. that the regional stress is 1–10 times the earthquake stress drop), large rotations are restricted close to the fault rupture, where the earthquake stress change is significant relative to the regional stress. Positive optimally oriented stress changes are seen along the fault in Fig. 3(b) where the fault slip exceeded 6 m (as seen in Fig. 1b), but such positive changes apply to planes which strike at a high angle to the North Anatolian fault. Far from the 1939 rupture, rotation of the optimal planes is negligible. For an apparent coefficient of friction  $\mu'$  of 0.4 in this stress field, it is seen that right-lateral faults striking east–west, such as the North Anatolian, are optimally oriented (Figs 2b and 3b). Coulomb stress changes on optimally oriented planes are also plotted for a decade of secular stress build-up in Fig. 2(b). Here the rotations are negligible because the stress per decade, about 1.5 bar, is small relative to the 100-bar regional stress. A complete description of this method, and its dependence on friction and the regional stress, is given in King *et al.* (1994).

To summarize, we use the optimally oriented Coulomb stress changes to visualize stress transfer, because the patterns are simpler, and because they do not depend on knowledge of the faults surrounding the source. Such figures also show the correspondence between regions of calculated stress change and background seismicity or aftershocks (Figs 4g and 5), because small shocks can occur on small faults, which could take any orientation consistent with the regional stress. But for calculations of triggering, time advance, and earthquake probability, we use the resolved stress changes as shown in Fig. 3(a) and as listed in the tables.

## STRESS EVOLUTION DURING THE SEQUENCE

The build-up of stress at successive rupture sites, as well as the competition between secular stress accumulation and earthquake stress drop are illustrated by sequential plots of the

**Figure 1.** (a) Active faults in Turkey (Sengor, Gorur & Saroglu 1985; Barka 1992; Saroglu & Kuscu 1992), with the North Anatolian fault in bold. GPS observations establish a  $24 \pm 4$  mm yr<sup>-1</sup> ( $1\sigma$  confidence) deep slip rate on the North Anatolian fault and reveal that the right-lateral transform describes a small circle about a ( $33.4 \pm 0.5^\circ$ E,  $31.1 \pm 1.3^\circ$ N) Anatolia–Eurasia rotation pole, which lies at the intersection of the dashed red lines (Oral 1994). (b) Cumulative right-lateral slip associated with  $M \geq 6.7$  earthquakes (Barka & Eyidogan 1993; Barka 1995; Bennet *et al.*, in preparation); the sequence ruptured from warm to cool colours. Slip in the 1949, 1966, and 1971 shocks is approximate, and the reverse-slip component for the Ezine and Kursunlu faults is not shown. (c) The region inscribed by the solid red line in (a) is projected relative to the Anatolia–Eurasia rotation pole, so that a transform fault would strike due east–west; the North Anatolian fault is seen to deviate less than 40 km from being a simple right-lateral transform.

**Figure 2.** Secular slip model used to calculate the loading of the North Anatolian fault system. (a) Steady deep slip below 12.5 km, as inferred from GPS observations (Le Pichon *et al.* 1993; Oral 1994; Oral *et al.* 1997; Straub & Kahle 1994; Straub 1996), transfers stress to the seismogenic portion of the fault. The model shown, projected relative to the pole of rotation as in Fig. 1(c), is used for the Coulomb stress changes on optimally oriented faults (Figs 3, 4 and 5); an identical model projected in UTM coordinates, as in Fig. 1(a), is used for the stress changes resolved on specific faults (Tables 1–3). (b) The secular stress rate is resolved on the fault at the indicated points, and also calculated for optimally oriented vertical strike-slip faults (colour gradients). Deep slip and stress are distributed between two strands at the west end of the fault.

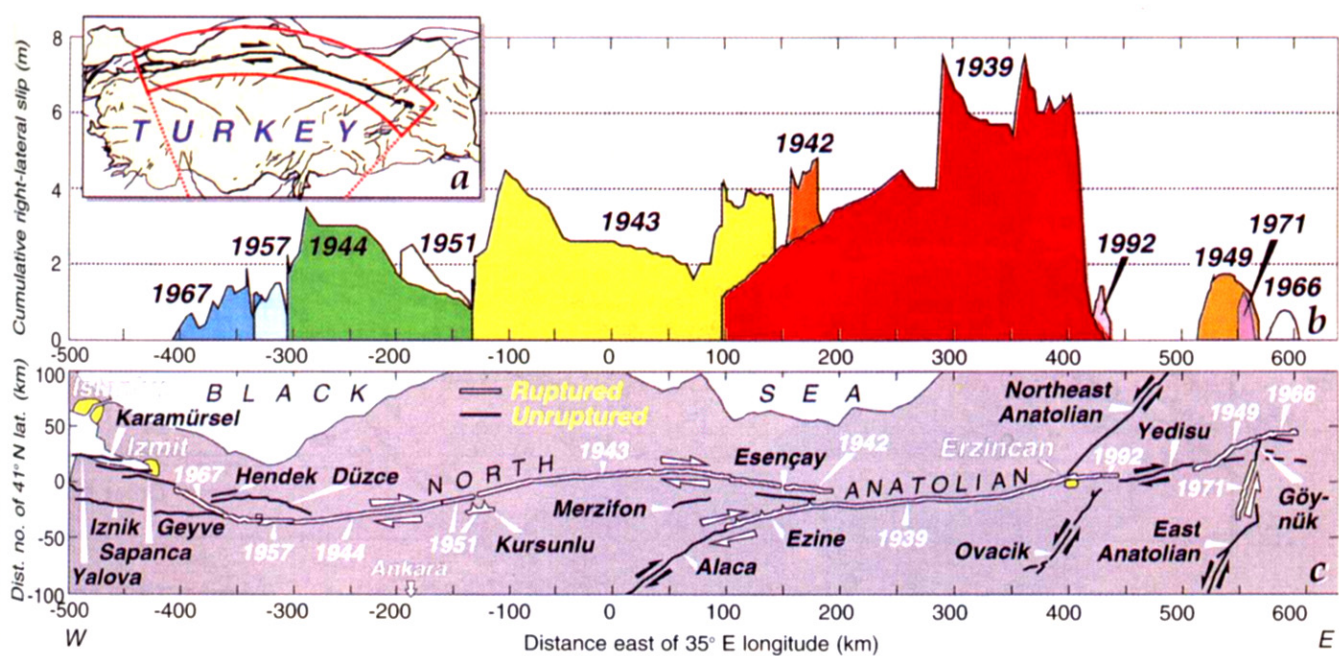


Figure 1.

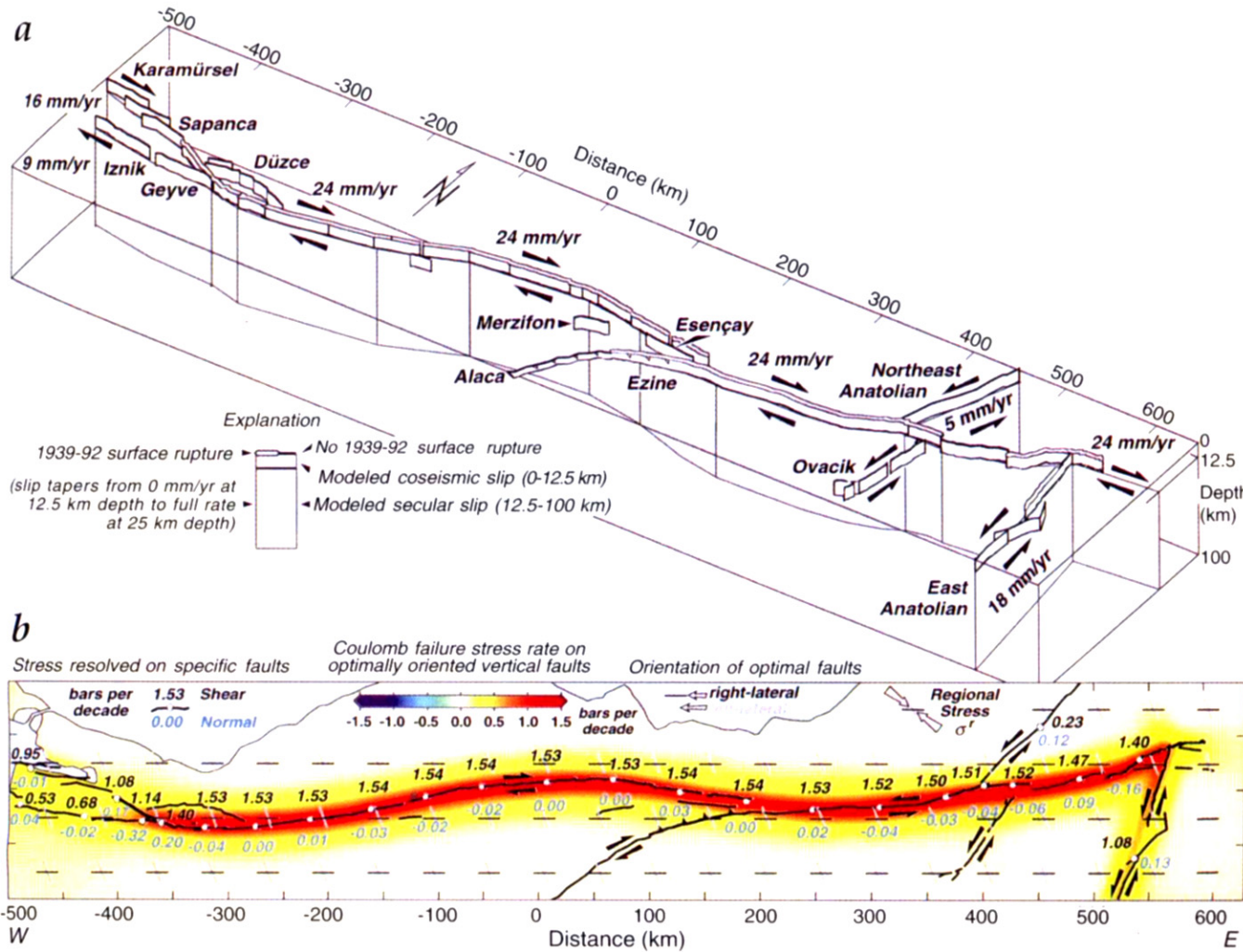
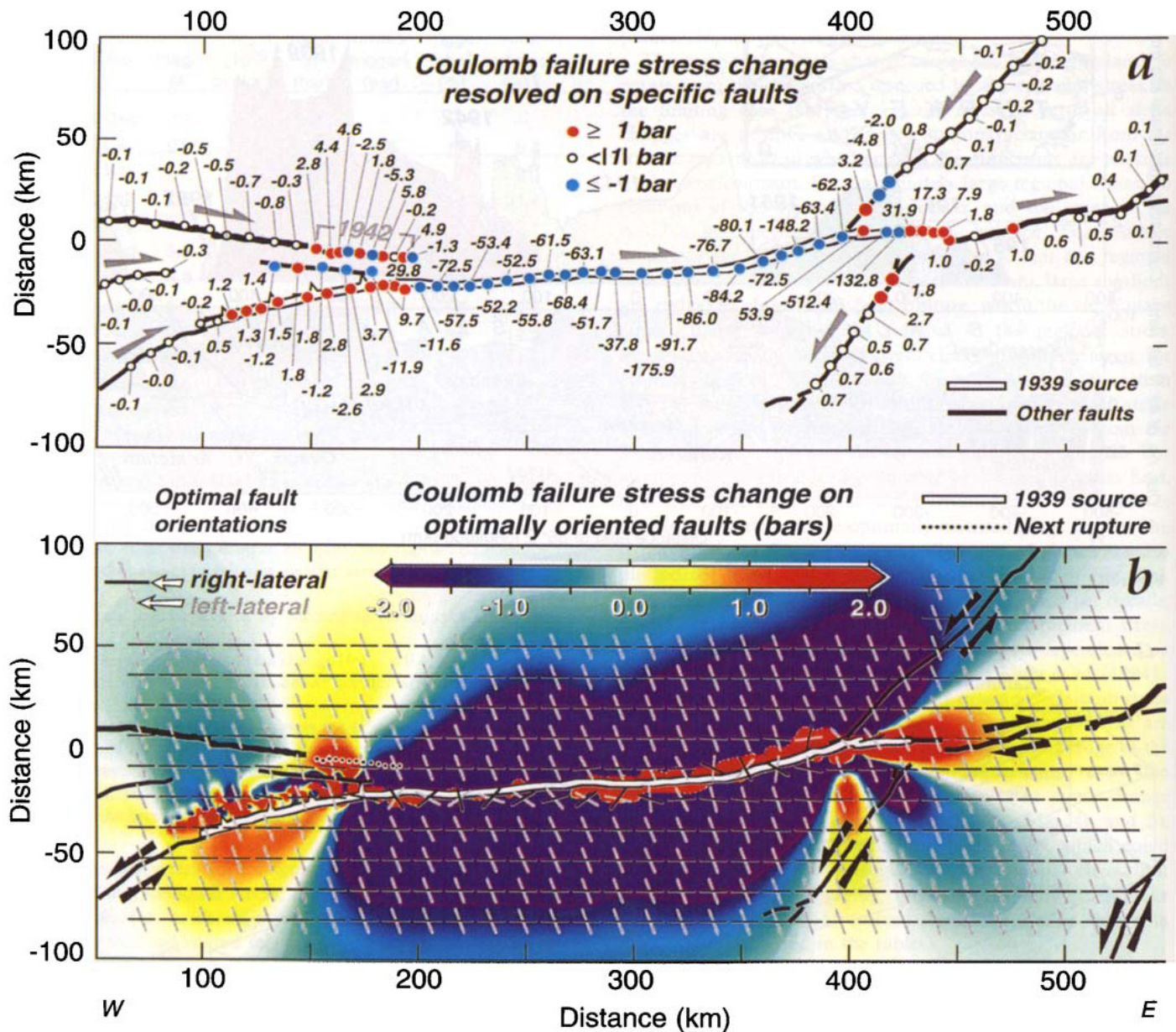


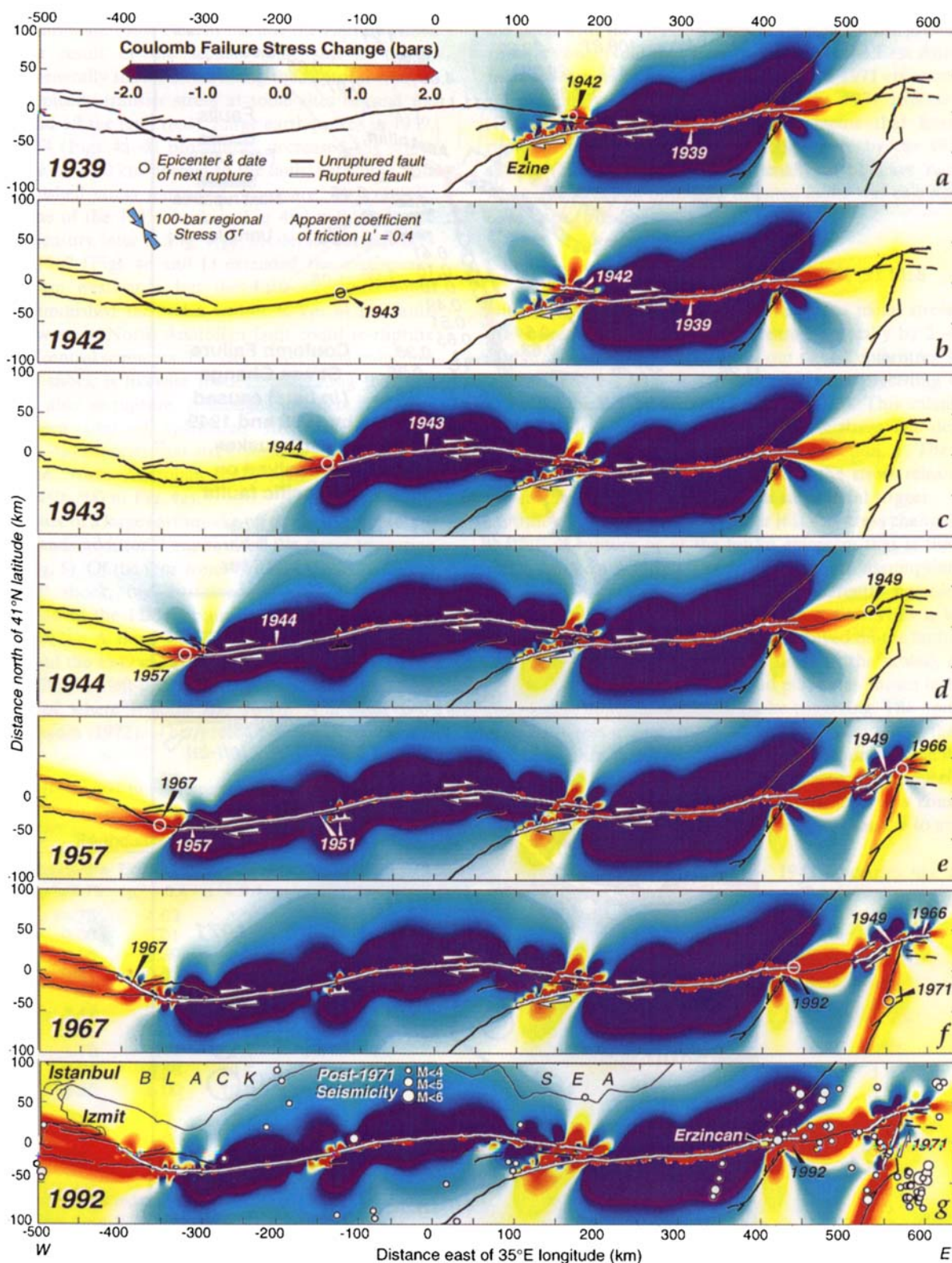
Figure 2.





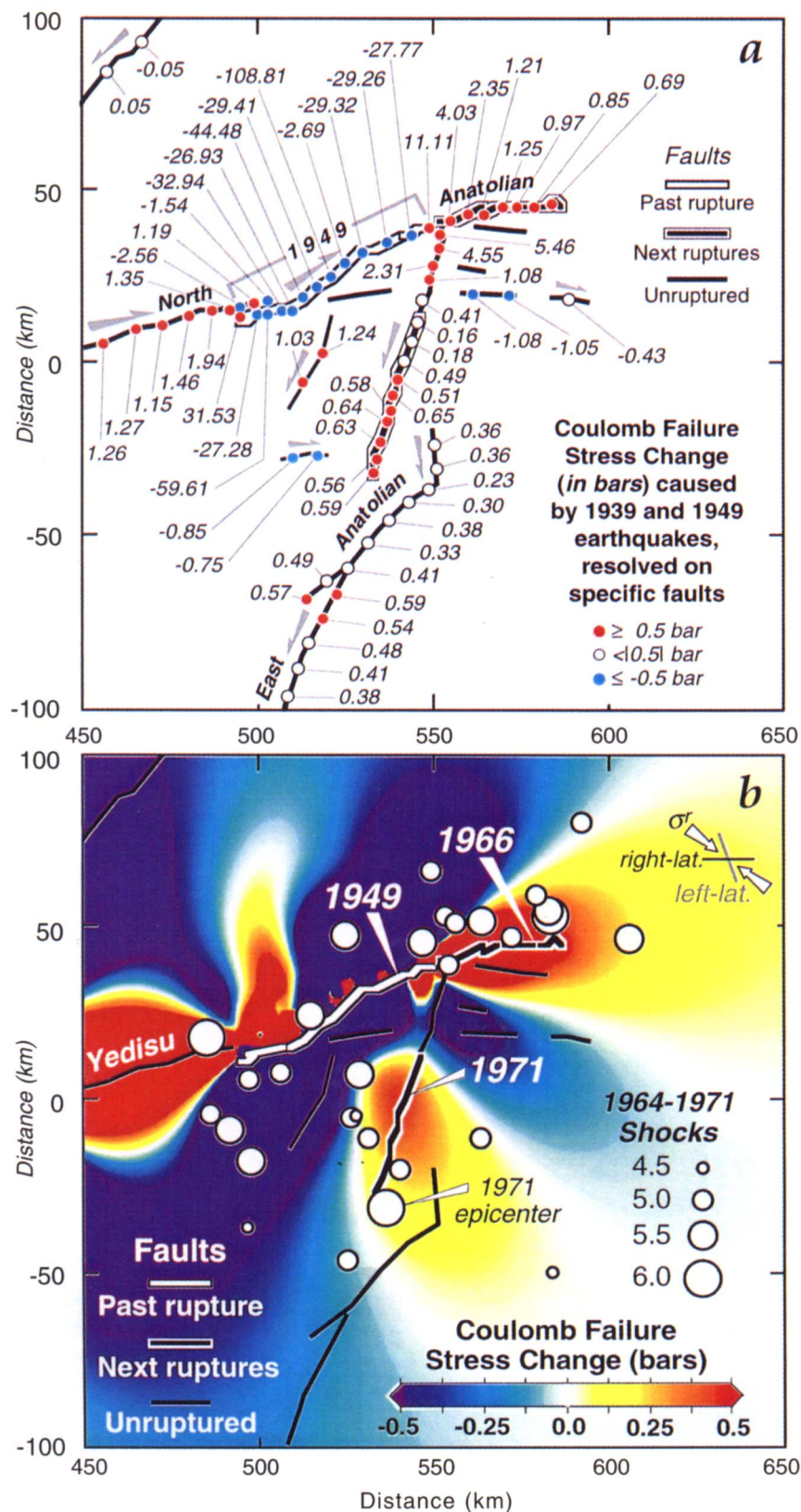
**Figure 3.** Stress changes associated with the 1939 earthquake. (a) Coulomb stress change on major faults caused by the 1939 earthquake. Stress is resolved on the fault surface, projected in UTM coordinates, at a depth of 8 km. Faults are assumed to be vertical, except for the west end of the 1939 rupture, which dips  $50^\circ$  N. No information about the regional stress is needed for this calculation. The mean stress change along the future 1942 rupture is +1.4 bars. (b) Colour gradients show the Coulomb stress change on optimally oriented vertical strike-slip faults at a depth of 8 km. The calculation assumes that the regional stress is 100 bars compression oriented  $55^\circ$  clockwise from the local Anatolian fault strike. Large rotations of the optimal planes occur close to the fault rupture, where the earthquake stress change is significant relative to the regional stress. Far from the 1939 rupture, rotation of the optimal planes is negligible.





**Figure 4.** Cumulative stress changes caused by large earthquakes and steady deep slip on the North Anatolian fault since 1939. In each panel, the epicentre of the next earthquake to rupture is circled. All but the 1943 epicentre lie in regions where the stress rose significantly, typically by 2–5 bars, owing to the foregoing shocks and deep fault slip. Relocated ISC earthquakes (Engdahl *et al.* 1996) are shown in g, with the 1992 Erzincan aftershock sequence removed. Calculations are made in an elastic half-space with a shear modulus of  $3.15 \times 10^{11}$  dyne  $\text{cm}^{-2}$  and a Poisson's ratio of 0.25. Earthquake slip is assigned as in Fig. 1(b), assumed to be uniform over 0–12.5 km depth. The fault was digitized and stress was sampled at 5 km increments, and is projected as in Fig. 1(c) so that the regional stress maintains a nearly fixed angle to the fault.





**Figure 5.** Stress changes at the end of the North Anatolian fault caused by 1939 and 1949 earthquakes (Ambraseys 1988). To emphasize the earthquake stress transfer, secular stress accumulation is not included in this plot; its inclusion would simply raise the stress along the North and East Anatolian faults by 1–1.4 bars. Projection as in Fig. 4. (a) The 1939 and 1949 earthquakes highly stress the sites of the future 1966 and 1971 earthquakes. Most segments that did not subsequently rupture were brought further from failure, except for the Yedisu segment. (b) Most aftershocks or small earthquakes occur in regions where the stress change on optimally oriented strike-slip faults was raised by the 1939–1949 earthquakes. The optimal orientations for right- and left-lateral faults off the 1949 rupture zone are shown with the assumed regional stress direction,  $\sigma$ . Earthquakes from 1964 from Engdahl *et al.* (1996) are shown, rather than from 1949, because of the poor network quality before 1964.

Coulomb stress change (Fig. 4). The stress increase along the North Anatolian fault, most evident outside the rupture zones (yellow), is a result of the secular fault slip at depth. Earthquakes generally relieve stress along the ruptures (purple zones), and typically transfer stress at some sites beyond the rupture tips and off the fault (red). Large earthquakes in 1939, 1943, and 1944 (Figs 4a–d) profoundly decreased the stress over a distance of  $\sim 50$  km normal to the fault; with time, this zone of diminished stress narrowed. Compare, for example, the purple zone of the 1943 shock in Fig. 4(c) with the same region half a century later in Fig. 4(g). Moderate earthquakes in 1957 and 1967 (Figs 4e and f) extended the earthquake sequence 100 km westwards, but these shocks redistributed rather than diminished the stress within 50 km of the fault, and thus the western North Anatolian fault could re-rupture long before its central segments. The calculated stress reduction near the 1942 shock is likewise modest, suggesting that this section could also re-rupture. Although imperfect, the correlation between sites of calculated stress increase and seismicity (Fig. 4g) suggests that stress remains high at several sites along the North Anatolian fault, such as the Yedisu segment (km 450–500 in Fig. 4g).

The occurrence of a large earthquake off the North Anatolian fault in 1971 lends additional support for the stress-triggering hypothesis (Fig. 5). Of the four zones brought closer to failure after the 1949 shock, two sustained  $M \geq 6.7$  earthquakes (beyond the end of the 1949 rupture in 1966, and in an off-fault lobe in 1971). A third site sustained an  $M = 5.6$  shock (in 1967) beyond the 1949 rupture at the east end of the Yedisu segment (Fig. 5b). The left-lateral East Anatolian fault ruptured 50 km south of where it joins the North Anatolian fault (Seymen & Aydin 1972). The preceding North Anatolian

earthquakes increased stress on the East Anatolian fault by 0.6 bars, with the stress maximum centred on the future 1971 rupture zone. Note that stress resolved on the East Anatolian fault reaches its maximum near the future 1971 epicentre, and remains above 0.5 bars for most of the 1971 rupture zone (Fig. 5a). In addition, most fault segments that have not ruptured were brought farther from failure by the 1939–49 shocks (Fig. 5a). Finally, most small earthquakes occurred where the stress on optimally oriented faults was calculated to have risen (Fig. 5b).

## STRESS AT FUTURE RUPTURE SITES

Nine out of 10 shocks occurred where the mean stress over the entire future rupture had increased, typically by 2–4 bars (Table 2, col. 4). Similarly, nine out of 10 epicentres struck where the stress had been increased by the preceding earthquakes, typically by 3 bars (Table 2, col. 3). This calculation is independent of the regional or tectonic stress, and depends only on the fault slip, geometry, and the friction,  $\mu'$ . The stress transfer averages about 20 per cent of the stress released by the earthquakes (Table 1, col. 7), a substantial trigger.

Although it is unknown whether it is the stress change along the future rupture or at the future epicentre that is the most important to triggering, the results for both assumptions are quite similar (Table 2). Faults are inherently complex, en échelon, and multi-stranded on many scales. Thus it is also unknown whether the stress change resolved on the fault plane as defined by its surface trace (as listed in the tables), or the stress change on optimally oriented planes (as shown in Fig. 4) is the most important to earthquake triggering. The optimally oriented stress increases are about 25 per cent larger than the resolved stress changes. Thus despite uncertainty in identifying the stress component that is most effective in triggering or advancing future earthquakes, the results lead to a consistent finding that the transfer of stress by one earthquake to another promoted the Anatolia sequence.

Scholz (1990) argued that the 1943 epicentre lies at the 'wrong' end of the 1943 rupture, because the epicentre locates

Table 2. Stress transfer to future ruptures.

Triggered Event	Coulomb failure stress change (bars)				
	Earthquakes only			Earthq.+secular	
	Epicentre $\mu' = 0.75$	Epicentre $\mu' = 0.4$	Mean $\mu' = 0.4$	Epicentre $\mu' = 0.4$	Mean $\mu' = 0.4$
1942	11.75	4.63	1.3	4.7	1.5
1943	0.00	0.01	-0.0	0.6	0.6
1944	6.56	6.39	4.8	7.3	5.6
1949	0.61	0.53	0.3	1.3	1.4
1951	1.49	1.71	1.7	1.7	1.7
1957	3.47	3.45	4.0	5.4	5.9
1966	3.85	4.03	3.0	8.2	5.4
1967	1.70	1.47	1.4	4.4	4.3
1971	0.71	0.58	0.5	3.5	3.2
1992	9.60	8.00	19.0	16.0	31.6
Average	4.0	3.1	3.7	5.2	6.1
min/max excluded	3.5	2.9	2.0	4.4	3.6

Cumulative stress transferred by  $M \geq 6.7$  earthquakes and by secular stress accumulation since 1939, resolved onto future ruptures at 8 km depth. Faults were digitized at 5 km increments, with calculations performed with the fault projected in UTM coordinates, as in Fig. 1a. The stress change shown for the 1942 earthquake assumes that the Ezine fault (Fig. 1c) has a  $50^\circ$ N dip and a 1:1 right-reverse-slip component (if the Ezine is treated as a vertical strike-slip fault, the mean change on the 1942 rupture zone is  $-6.0$  bars and the epicentral change is  $-3.0$  bars). The stress transferred by the 1951 earthquake is calculated for the  $60^\circ$ N-dipping Kursunlu thrust fault (Pinar 1953), although the epicentre could lie on the North Anatolian fault. The epicentral stress for  $\mu' = 0.75$  gives results for low pore fluid pressure.

Table 3. Stress on unruptured faults.

Fault	Coulomb stress change (bars)			
	Earthquakes		Earthq.+secular	
	Max	Mean	Max	Mean
Yalova	0.03	0.02	1.3	1.3
Sapanca	0.5	0.2	1.6	1.3
Geyve	2.6	-1.6	6.7	2.5
Hendek	1.6	0.8	1.8	1.0
Düzce	2.3	-2.5	4.1	-0.7
Merzifon	-0.3	-1.4	0.4	-0.7
Alaca	3.0	0.2	3.0	0.2
Esençay	-3.7	-9.8	3.6	-2.5
Ovacik	8.0	1.8	7.6	1.7
NE Anat.	0.9	-0.3	0.1	-0.8
Yedisu	2.3	1.4	10.1	9.2
Göynük	5.4	3.5	8.1	6.2
Average	1.9	-0.6	4.0	1.6
min/max excluded	1.8	-0.1	3.8	1.2

Calculated stress transferred by  $M \geq 6.7$  earthquakes and secular accumulation during 1939–1995, for  $\mu' = 0.4$ , resolved onto unruptured faults, listed from west to east (see Figs 1c and 3g).



at the end of the rupture farthest from the preceding 1942 shock. However, the calculated stress change at the end of the 1943 rupture closest to the 1942 shock inhibited failure (Fig. 3), and the 1943 epicentre lies within 40 km of where the stress change is most positive (Figs 3a and b). Only the 1949 earthquake struck farther from the stress maxima associated with the preceding shocks (Fig. 2d), which is surprising because the intervening Yedisu segment last ruptured in 1784, and so the accumulated stress should have been high. Seismicity is now concentrated along this segment (Fig. 3g). The much better located aftershocks of the 1992 earthquake lie in regions of calculated failure stress increase (Nabiant, Barka & Alptekin 1996).

Most fault segments that sustained stress decreases have not ruptured, a further indication that stress changes influence earthquake occurrence. The typical stress change for the dozen unruptured segments since 1939 is  $-0.1$  to  $-0.6$  bars (Table 3, col. 2), in comparison with a 2–4 bar increase for those that have ruptured (Table 2, col. 3). Even when the secular stress accumulation during 1939–95 is included, the stress changes on the unruptured segments facilitated failure by only 1.2–1.6 bars (Table 3, col. 4), in comparison with a 3.6–6.1 bar increase for the segments that ruptured (Table 2, col. 5).

## EARTHQUAKE PROBABILITIES

The effect of the stress change on times of earthquake recurrence can be cast as a change in the probability of future events. The times of future earthquakes along a fault segment are uncertain because of intrinsic variability of the earthquake faulting process and uncertainty of the observations used to estimate recurrence time. Estimations of the probability of future events over a given time interval provide the means to account for these uncertainties. Departing from previous studies, which consider only a permanent effect of stresses on segment probabilities (Cornell *et al.* 1993; Working Group on California Earthquake Probabilities 1990; Working Group on the Probabilities of Future Large Earthquakes in Southern California 1992), we consider both permanent and transient effects of the stress changes on earthquake probabilities.

### Segment probability prior to a stress step

Two models for the estimation of earthquake probabilities are in general use, the stationary Poisson model and the conditional probability model (Cornell & Winterstein 1988; Hagiwara 1974). The conditional probability model can be tailored to find the effects that elapsed time and stress changes have on earthquake probabilities. We first present results from the simple Poisson model for comparative purposes and for later use in addressing transient effects of stress changes on probabilities. The stationary Poisson model assumes that the probability of an earthquake in a time interval is independent of the elapsed time from previous events. The probability of at least one event in the interval  $\Delta t$  is

$$P = 1 - \exp(-r\Delta t) = 1 - \exp(-N), \quad (2)$$

where  $r$  is a constant occurrence rate for earthquakes that rupture the segment of interest and  $N$  is the expected number of such events in the interval  $\Delta t$ .

With the conditional probability model, probability can increase with time to represent increasing stress on a fault

segment towards an uncertain stress threshold. We estimate the probability for recurrence of an earthquake on a fault segment prior to the stress step, given an elapsed time  $t$  from the previous earthquake, following the method of the Working Group on California Earthquake Probabilities (1990). The probability for recurrence of slip in any time interval  $(t, t + \Delta t)$  is

$$P(t \leq T \leq t + \Delta t) = \int_t^{t+\Delta t} f(t) dt, \quad (3)$$

where  $f(t)$  is the probability density function for the uncertain recurrence time  $T$  for a segment-rupturing earthquake. The probability, conditional on the earthquake not occurring prior to  $t$ , is

$$P(t \leq T \leq t + \Delta t | t > T) = \frac{P(t \leq T \leq t + \Delta t)}{P(t \leq T \leq \infty)}. \quad (4)$$

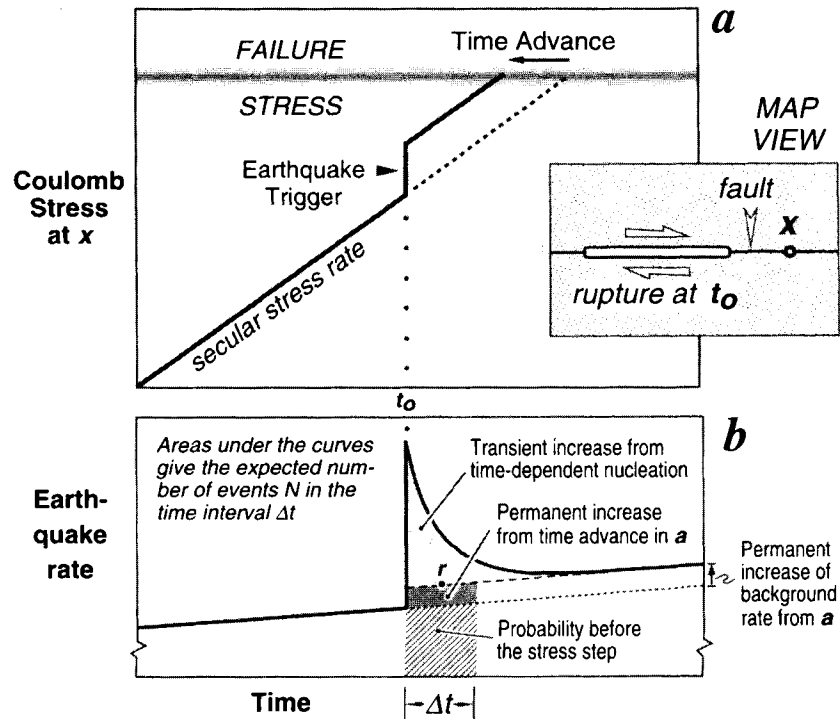
We assume a lognormal probability distribution of recurrence times,

$$f(t) = \frac{1}{MS\sqrt{2\pi}} \exp\left\{-\frac{[\ln(t/M)]^2}{2S^2}\right\}, \quad (5)$$

where  $M$  is the median and  $S$  is the standard deviation of the natural logarithm of the random recurrence time.

To estimate probabilities, we require values for  $M$  and  $S$ , as well as the time elapsed  $t$  during the 1939–67 sequence. Recall that for the log normal distribution,  $S^2 = \ln(s^2/m^2 + 1)$  and  $M = m \exp(-\frac{1}{2}S^2)$ , where  $m$  and  $s$  are the mean and standard deviation of the recurrence time. Because the observations are sparse and uncertain, we do not distinguish different repeat times along the North Anatolian fault; instead we use the portions of the fault for which the record is longest to estimate a generic repeat time (see Fig. 7). Although segment probabilities are sensitive to  $m$ ,  $s$  and  $t$ , we show that probability gains associated with the stress steps (the ratios of probability after the steps to the probability before the steps) are insensitive to parameter choices. In the west (at about  $\text{km} = -200$  in Fig. 7), earthquakes struck in 1035 AD, 1668, and 1944. For the central region, at  $\text{km} = -50$ , events occurred in 1050 AD, 1668, and 1943. For the eastern region near Erzincan at  $\text{km} = 350$ , earthquakes took place in 1043 AD, 1254, and 1939 (Ambraseys 1970; Ikeda *et al.* 1991; Ambraseys & Finkel 1995). Together these yield  $m = 450$  yr, with  $s = 220$  yr. The derived coefficient of variation of 0.5 is in accord with observations for faults with longer palaeoseismic records, such as the southern San Andreas (Working Group on California Earthquake Probabilities 1995). The time  $t$  elapsed between the 1939–67 sequence and the previous events in 1254–1668 is taken to be  $\sim 425$  yr (a weighted average) in a  $450 \pm 220$  yr cycle. For the Poisson calculation (eq. 2) the earthquake rate  $r$  is taken as  $1/m$ . The stressing rate in our model is  $0.15 \text{ bar yr}^{-1}$  along most of the North Anatolian fault system (Fig. 2b).

The fault slip rate of  $24 \text{ mm yr}^{-1}$ , an average secular stressing rate of  $0.15 \text{ bar yr}^{-1}$ , and a repeat time of 450 yr give a mean slip of 11 m per event and a mean stress drop of 68 bars. During the twentieth century, the slip and stress drops are lower than this estimate, except for the 1939 earthquake, suggesting that we may have overestimated the repeat time and thus underestimated the earthquake probability. This could arise if some large earthquakes are missing from the historical record. To examine the impact of overestimating the repeat time, and to define a range of probabilities appropriate



**Figure 6.** Schematic illustration of a sudden stress increase  $\Delta\sigma_r$  on a fault at point  $x$  near an earthquake rupture at time  $t_0$  (inset). (a) The stress increase advances the time to the next rupture. If the stress were closer to failure at the time of the stress step, the trigger might have triggered an earthquake immediately. (b) The associated short-term (transient) and long-term (permanent) probability gain (Dieterich & Kilgore 1996). The transient gain (curved portion of solid line) scales with the rate of aftershock decay, and the permanent gain (dashed to solid line) is typically a factor of 1.12 higher than the probability before the triggers in the Anatolian sequence.

to the observations, we also calculate probabilities using an alternative set of parameters. We arbitrarily halve the repeat time, leaving the coefficient of variation at 0.5. Thus  $m = 225$  yr and  $s = 110$  yr. For the elapsed time in these calculations we use the time since the great 1668 earthquake (Fig. 7), so  $t = 271$  yr. The mean recurrence time of 225 years gives a mean event slip of 5.4 m per event and a mean stress drop of 34 bars.

For the time interval used in this study,  $\Delta\tau = 10$  yr, the first set of parameters ( $m = 450$  yr,  $s = 220$  yr,  $t = 450$  yr) give generic segment probabilities of 0.022 and 0.036 for the Poisson and conditional probability models, respectively, and the second set of parameters ( $m = 225$  yr,  $s = 110$  yr,  $t = 271$  yr) give generic segment probabilities of 0.044 and 0.130 for the Poisson and conditional probability models, respectively. Because the elapsed times are close to the mean recurrence times, the conditional probabilities are larger than the Poisson probabilities for both parameter sets.

#### Permanent effect of stress change

Increasing (or decreasing) the Coulomb stress on a fault segment permanently shortens (or lengthens) the time required for tectonic stressing to bring a segment to failure (Fig. 6a), and thus causes a permanent change in conditional probability. The conditional probability model can be adapted to estimate the effect of stress changes by equating a stress change with the time required to accumulate stress through secular stressing.

Two very similar methods have been proposed to estimate the effect of a stress increase on the conditional probability. The first method advances the elapsed time in the conditional probability calculation (eqs 3–5) from  $t$  to  $t'$  by the equivalent

time required to accumulate the stress step  $\Delta\sigma$  through the secular stressing process (Dieterich 1988):

$$t' = t + \frac{\Delta\sigma}{\dot{\sigma}}, \quad (6)$$

where  $\dot{\sigma}$  is the tectonic stressing rate. The second approach reduces the expected mean recurrence time from  $m$  to  $m'$  by the equivalent time required to accumulate the stress step through the secular stressing process (Working Group on California Earthquake Probabilities 1990):

$$m' = m - \frac{\Delta\sigma}{\dot{\sigma}}. \quad (7)$$

Reducing  $m$  or increasing  $t$  for a positive step in stress increases the conditional probability of an earthquake (Fig. 6b, dotted to dashed lines). We have employed eq. (7) in computing conditional probabilities following a stress step, because it is consistent with the concept that recurrence time is reduced by a step increase in stress. Both methods yield similar results, although eq. (7) yields larger changes of probability for a given stress step. Segment probabilities following the stress step are given in Table 4 (col. 5) for the first parameter set, and in Table 5 (col. 5) for the second parameter set.

#### Transient effect of stress change

The existence of foreshocks and aftershocks demonstrates that when an earthquake occurs there is a large transient increase in the probability of additional earthquakes in the surrounding area. Similarly, global statistics of earthquake pairs reveal strong clustering in space and time, in which the occurrence

Table 4. Triggered earthquake probabilities ( $450 \pm 220$  yr repeat time).

Triggered Shock Year	Date	Probability before the stress step		recurrence* time change	Probability after the stress step†		Probability gain
		Poisson	Conditional †	(yr)	Permanent effect	Transient + perm. effect	(col. 7+ col. 4)
1942	20 Dec	0.022	0.036	-8.4	0.038	0.074	2.0
1943	26 Nov	0.022	0.036	0.0	0.036	0.036	1.0
1944	1 Feb	0.022	0.036	-31.4	0.041	0.204	5.6
1949	17 Aug	0.022	0.036	-2.1	0.037	0.044	1.2
1951	13 Aug	0.022	0.036	-11.0	0.038	0.087	2.4
1957	26 May	0.022	0.036	-28.6	0.041	0.174	4.8
1966	19 Aug	0.022	0.036	-30.0	0.041	0.140	3.9
1967	22 Jul	0.022	0.036	-12.3	0.038	0.078	2.1
1971	22 May	0.022	0.036	-4.6	0.037	0.050	1.4
1992	13 Mar	0.022	0.036	-125.0	0.059	0.704	19.4
<b>Average</b>				<b>-25.3</b>	<b>0.041</b>	<b>0.159</b>	<b>4.9</b>
<b>Average (min/max values excluded)</b>				<b>-16.1</b>	<b>0.039</b>	<b>0.105</b>	<b>2.9</b>

† Elapsed time is assumed to be 425 yr (weighted average time since complete rupture of the North Anatolian fault in earthquakes during 1254 and 1668; see Fig. 7).

\* From eq. (7), using the stress transfer in Table 2 (col. 4) divided by the secular stressing rate for each rupture zone ( $0.10\text{--}0.15$  bar  $\text{yr}^{-1}$ ) as shown in Fig. 2(b).

‡ This uses the stress-modified recurrence time to compute the conditional probability for the ten years after the stress step.

Table 5. Triggered earthquake probabilities ( $225 \pm 110$  yr repeat time).

Triggered Shock Year	Date	Probability before the stress step		recurrence* time change	Probability after the stress step†		Probability gain
		Poisson	Conditional †	(yr)	Permanent effect	Transient + perm. effect	(col. 7+ col. 4)
1942	20 Dec	0.043	0.130	-8.4	0.136	0.254	2.0
1943	26 Nov	0.043	0.130	0.0	0.130	0.130	1.0
1944	1 Feb	0.043	0.130	-31.4	0.155	0.599	4.6
1949	17 Aug	0.043	0.130	-2.1	0.131	0.156	1.2
1951	13 Aug	0.043	0.130	-11.0	0.138	0.296	2.3
1957	26 May	0.043	0.130	-28.6	0.152	0.533	4.1
1966	19 Aug	0.043	0.130	-30.0	0.154	0.453	3.5
1967	22 Jul	0.043	0.130	-12.3	0.139	0.296	2.1
1971	22 May	0.043	0.130	-4.6	0.133	0.175	1.3
1992	13 Mar	0.043	0.130	-125.0	0.252	0.996	7.7
<b>Average</b>				<b>-25.3</b>	<b>0.152</b>	<b>0.386</b>	<b>3.0</b>
<b>Average (min/max values excluded)</b>				<b>-16.1</b>	<b>0.142</b>	<b>0.342</b>	<b>2.6</b>

† Elapsed time is assumed to be 271 yr (time since the great 1668 earthquake in Fig. 7).

\* From eq. (7), using the stress transfer in Table 2 (col. 4) divided by the secular stressing rate for each rupture zone ( $0.10\text{--}0.15$  bar  $\text{yr}^{-1}$ ) as shown in Fig. 2(b).

‡ This uses the stress-modified recurrence time to compute the conditional probability for the 10 yr after the stress step.

of one earthquake increases the probability of a second earthquake, with the probability decaying with time and distance from the first event (Kagan & Jackson 1991). These transient increases of earthquake probabilities are among the most prominent of statistical features of earthquake occurrence. A quantitative and unified explanation of aftershock distributions and decay, global clustering statistics, and foreshock statistics, is given by a single model in which the rate of earthquake occurrence is perturbed by the local stress increase caused by a prior earthquake (Dieterich 1994; Dieterich & Kilgore 1996). We employ this model to calculate this transient change of the segment earthquake probabilities.

The model is based on the constitutive formulation for the rate of earthquake activity proposed by Dieterich (1994), derived from laboratory observations of rate- and state-dependent fault properties. The rate and state dependence of fault properties has been observed for a diverse variety of materials over the range of conditions for crustal earthquakes. Numerical simulations using these fault constitutive properties

reproduce the full range of observed fault-slip phenomena, including laboratory observations of the spontaneous time-dependent nucleation of slip instabilities over a range of stresses above some minimum critical stress level, and healing following slip (Dieterich & Kilgore 1996). A consequence of clustering statistics and time-dependent nucleation is that earthquake rates at all magnitudes undergo a strong transient amplification at the time of a step increase of stress, followed by a  $1/t$  decay to their background rate (Fig. 6b).

Because the transient effect of the stress change is expressed as a change in expected rate of segment events, it is convenient to formulate the probability analysis as a non-stationary process in which

$$P_n = 1 - \exp\left(-\int_0^{\Delta t} R(t) dt\right) = 1 - \exp(-N), \quad (8)$$

where,  $P_n$  is the net probability, which combines the transient and permanent effects of the stress change on earthquake



probability and  $R(t)$  is now a non-constant (decaying) earthquake rate following a stress step.  $\Delta t$  is measured from the time of the stress step; we use 10 yr for these computations. To evaluate eq. (8), we obtain  $N$ , by integrating the solution for  $R(t)$  following a stress step (Dieterich 1994; his eq. 12). For the interval 0 to  $\Delta t$ , this yields

$$N = r \left\{ \Delta t + t_a \ln \left[ \frac{1 + \left[ \exp \left( \frac{-\Delta\sigma_f}{A\sigma} \right) - 1 \right] \exp \left[ \frac{-\Delta t}{t_a} \right]}{\exp \left( \frac{-\Delta\sigma_f}{A\sigma} \right)} \right] \right\}, \quad (9)$$

where  $r$  is the permanent background component of the earthquake rate following the stress step (Fig. 6b),  $t_a$  is the characteristic duration of the transient effect, and  $\Delta\sigma_f$  is the calculated Coulomb stress change.  $A$  is a dimensionless fault constitutive parameter, and  $\sigma$  is the effective normal stress. Since  $t_a$  and  $A\sigma$  are unknown for the Anatolia sequence, we set  $t_a = 10.2$  yr, the value derived from pair clusters in the Harvard CMT global catalogue for  $M > 5$  earthquakes at depths  $< 70$  km, and  $A\sigma = 1$  bar from analyses of aftershocks and foreshocks (Dieterich 1994). Note that the transient effect disappears if  $\Delta\sigma_f = 0$ , in which case  $N = r\Delta t$ .

In eq. (9),  $r$  is the rate of activity implicit to the conditional probability following the stress step (Tables 4 and 5, col. 6). Hence, to evaluate  $r$  we equate the value of the conditional probability to a stationary Poisson probability and solve for  $r$ . From eq. (2),

$$r = (-1/\Delta t) \ln(1 - P), \quad (10)$$

where  $P$  is the previously obtained conditional probability for the fault segment following the stress step.

In summary, the net probability of events rupturing each fault segment (Tables 4 and 5, col. 7) combines both the permanent and transient effects of a stress step. The net probability is obtained by first computing the permanent effect of a stress change on the conditional probability using the approach of eq. (7). Then the equivalent Poisson rate  $r$  for the permanent effect is obtained using eq. (10) to evaluate eqs (8) and (9) for the net probability.

For completeness, we noted that eq. (9) assumes that the background rate  $r$  after the stress step is constant over the interval  $\Delta t$ , which it is not. Conditional probability grows slowly with elapsed time, requiring an increase of  $r$  with time (Fig. 6b). However, for the Anatolian computations the change of  $r$  over  $\Delta t = 10$  yr is small relative to the magnitude of  $r$ , and the resulting error introduced by this approximation is slight. In cases where  $\Delta t$  is large relative to the repeat time  $T$ , and where higher accuracy in the application of eq. (9) is sought, the time interval can be broken into  $n$  subintervals,  $\Delta t = \Delta t_1 + \Delta t_2 + \dots + \Delta t_n$ . The conditional probabilities  $P_i$  and expected number of events  $N_i$  are computed as before, for each subinterval  $i$ .  $P_n$  for the entire interval is then given by

$$P_n = 1 - [(1 - P_{n_1})(1 - P_{n_2}) \dots (1 - P_{n_n})], \quad (11)$$

where  $P_{n_1}$  etc. are the net probabilities obtained for each subinterval. Using the definition  $P_{n_i} = 1 - \exp(-N_i)$ , eq. (11) can be written as

$$P_n = 1 - \exp(-N), \quad (12)$$

where  $N = N_1 + N_2 + \dots + N_n$ .

## Net probability gain

The probability gain associated with the stress step is the net probability for some period after a stress increase, divided by the conditional probability prior to the step (Aki 1981). The probability gains for the two sets of parameters are listed in Tables 4 and 5 (col. 8). Note that, although net probabilities are very different for the two assumed repeat times, each set of recurrence parameters yields similar probability gains. It is also apparent that about 95 per cent of the 10 yr gain is caused by the transient effect. In other words, both aftershocks and subsequent main shocks are more likely in the stressed areas during the first decade after each large shock. We find an average three-fold gain in the probability of an  $M \geq 6.7$  earthquake during the decade after each triggering event, with a wide range for individual triggers of 1–19.

## LIMITATIONS OF THE ANALYSIS

Although we incorporate stress changes caused by earthquakes and secular fault slip, we make several assumptions that influence our results. Earthquake slip measured at the surface may under-represent the net slip at depth, and thus the stress change, by as much as 50 per cent. Surface slip occasionally exceeds the slip at depth, as at the north end of the 1992  $M = 7.4$  Landers, California, earthquake (Wald & Heaton 1994), so the calculated stress beyond the fault ends can also be too large. Our assumed 12.5 km depth of coseismic slip is consistent with the 1992 Erzincan earthquake (Barka & Eyidogan 1993; Nablant *et al.* 1996), but it is unknown for the preceding events. The deep slip rate used for the secular model is also uncertain by  $\pm 8$  mm yr<sup>-1</sup> (95 per cent confidence) (Oral 1994). In addition, we neglect two time-dependent effects: pore-fluid flow could raise  $\mu'$  with time, as suggested by Harris & Simpson (1992), Jaumé & Sykes (1992), and Scholz (1990), which would increase the stress changes by up to 25 per cent (Table 2, col. 2). Post-seismic asthenospheric relaxation also transfers stress to the upper crust. A 12.5 km thick elastic plate overlying an inviscid fluid approximates complete relaxation of the lower crust; this yields stresses twice as high and twice as broad as those calculated here (Stein, King & Lin 1992). Thus most processes we omit would, if included, increase the calculated stress transfer and associated probability gains.

Several assumptions introduce uncertainty into our probability calculations. To estimate the permanent stress effects, we used a common repeat and elapsed time for large earthquakes on the Anatolian fault, whereas repeat times for the better studied San Andreas fault differ by nearly a factor of 2 between the northern and southern segments. For the transient probability effects, we relied upon global average values for the key parameters because we lacked local information for Anatolia. Based on analyses of earthquakes elsewhere, these parameters could differ by  $\pm 50$  per cent. Fortunately, the probability gains listed in Tables 4 and 5 (col. 8) are less sensitive to these assumptions than the probabilities, particularly during the first decade after each triggering earthquake when transient effects are large.

## IMPLICATIONS FOR EARTHQUAKE FORECASTING

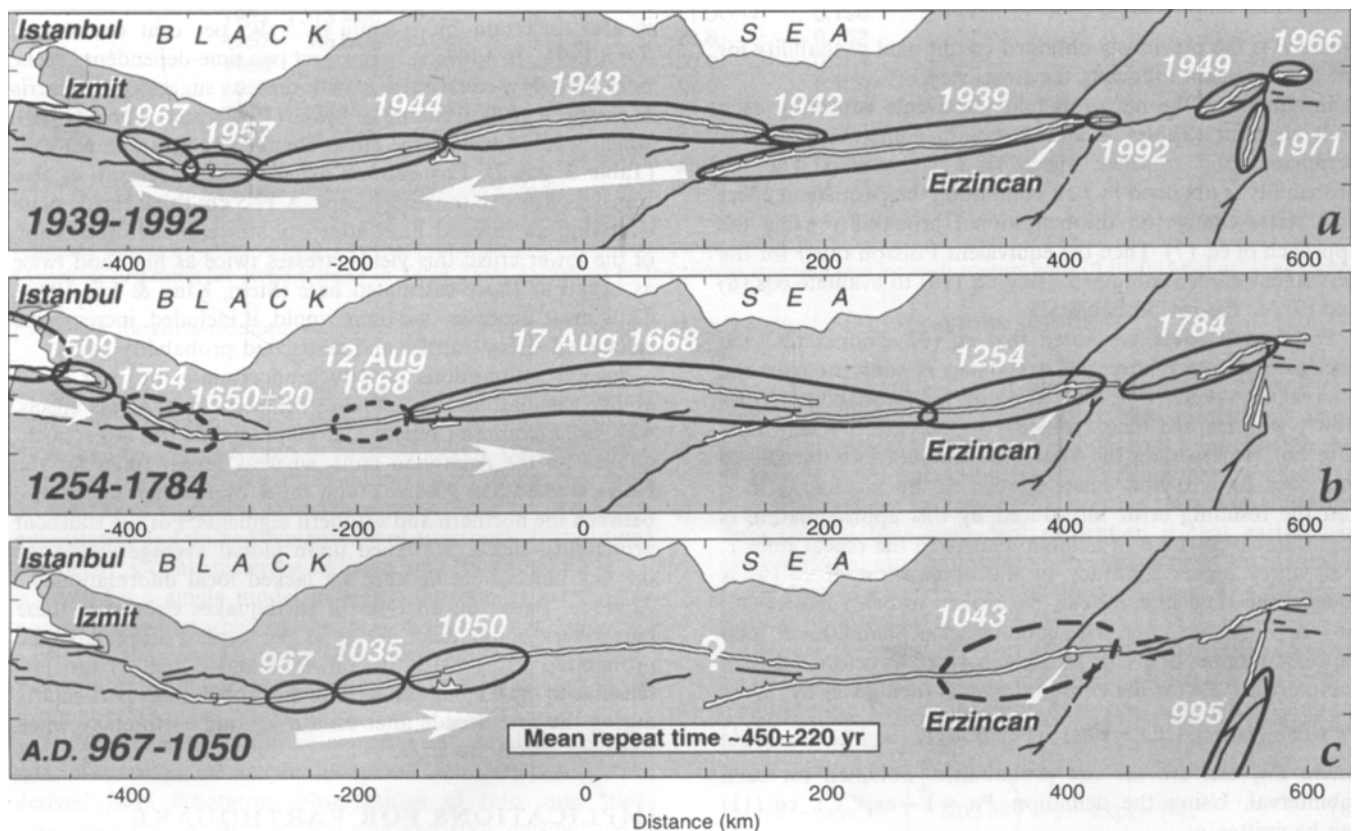
We identify several faults with a heightened probability of failure. The port city of Izmit is most vulnerable to an

earthquake on the Sapanca fault (Fig. 4g). Stress increases of 1.3–2.5 bars are found for the Geyve and Sapanca faults, which pose the greatest threat to Istanbul, particularly if the faults ruptured from east to west. The Sapanca fault last ruptured in 1878. We calculate a 30 yr probability during 1996–2026 for  $M \geq 6.7$  shocks on the Geyve and Sapanca fault segments to be 12 per cent; this probability is higher by a factor of 1.07 than the rate before these segments were stressed by the 1967 earthquake. The Yedisu (last rupture in 1784), Ovacik, and Göynük (last event in 1866) faults near Erzincan have been stressed towards failure by 1.7–9.2 bars. Erzincan, badly damaged during the 1939 and 1992 earthquakes, would be most affected if these faults ruptured towards the city (Fig. 4g). We calculate a 30 yr probability during 1996–2026 for  $M \geq 6.7$  shocks on the Yedisu segment to be 15 per cent; this is a factor of 1.35 higher than the rate before these segments were stressed by the 1992 Erzincan earthquake.

The Anatolian findings complement studies of the triggering of main shocks, aftershocks, and fault creep in California. The 1992  $M = 7.4$  Landers earthquake was calculated to have increased the stress by 1.5–3.0 bars where the  $M = 6.5$  Big Bear shock struck 3.5 hr after the Landers main shock, and 65 per cent of the Landers  $M \geq 1$  aftershocks occurred where the stress rose by  $>0.3$  bars (King *et al.* 1994). The Landers earthquake increased the stress 40 km away on the San Andreas fault by an estimated 2–6 bars (Harris & Simpson 1992; Jaumé & Sykes 1992; Stein *et al.* 1992), with  $\sim 150$  mm of slip needed to relieve the imposed stress (King *et al.* 1994). Subsequent

GPS (Shen *et al.* 1994) and continuous strain (Wyatt, Agnew & Gladwin 1994) measurements indicate that deep slip on the San Andreas fault of  $115 \pm 47$  mm occurred where the stress was calculated to have risen, and slip of  $-39 \pm 33$  mm occurred where the stress was calculated to have dropped, in close accord with the calculation. Stress changes associated with several other California earthquakes influenced subsequent seismicity (Jaumé & Sykes 1996; Harris & Simpson 1996; Harris *et al.* 1995; Simpson & Reasenber 1994; Stein *et al.* 1994). Together, these results attest that faults are sensitive to small but sustained stress changes transmitted over tens to hundreds of kilometres.

The North Anatolian fault has experienced several historical episodes of migrating earthquake sequences (Fig. 7). Large earthquakes progressed  $\sim 250$  km eastwards during 967, 1035, and 1050 AD (Ambraseys 1970). A sequence ruptured perhaps 700 km of the fault during  $1650 \pm 20$  to 1668 (Ikeda *et al.* 1991; Ambraseys & Finkel 1995). We suggest that the propensity of the fault zone towards progressive failure is a product of its simple, straight geometry, which, as seen in Fig. 4, makes for efficient transfer of stress; its isolation from other faults, which minimizes stress transferred between the North Anatolian and competing faults; and its en échelon character (Wesnousky 1988), which tends to keep the entire fault from rupturing at once (Fig. 1c). By contrast, the San Andreas fault, which lacks a historical record of progressive shocks, produces larger earthquakes along its smoother trace, and generally lies close to other major faults, making the stress transfer more irregular and complex.



**Figure 7.** Rupture zones for large historical earthquakes along the North and East Anatolian faults (Ambraseys & Finkel 1988, 1995; Ikeda *et al.* 1991; Barka 1992). Zones for earthquakes before 1939 are based largely on isoseismals, and are thus approximate. Earthquake progressions, indicated by arrows, occurred during three sequences but in different directions and at different rates.

## CONCLUSIONS

We find that earthquake-induced stress increases of several bars promoted the North Anatolian earthquake sequence, each shock raising the probability of future earthquakes at the site of the next-to-strike. Our analysis is least successful in explaining the occurrence of the 1943 earthquake and the absence of a Yedisu segment earthquake. Nor do we account for the time lag between individual triggers and ruptures, which varied from months to decades.

Our results suggest that earthquakes interact: when a large shocks occurs, it changes the conditions for failure in its vicinity, altering the probabilities for future events. In contrast, current approaches to earthquake hazard generally assume a stationary Poisson process where the past behaviour of large faults is unknown, in which earthquakes are assumed to occur randomly over time on a fault. Where more information is available, the time-predictable model (Shimazaki & Nakata 1980) is employed, in which the probability of an earthquake of specified size and location drops after the rupture but does not change elsewhere. Ward (1996) considered the permanent effects of stress transfer in a synthetic seismicity model for southern California, finding significant fault interactions, as we do here. Two seismic hazard analyses for the San Andreas system (Working Group on California Earthquake Probabilities 1990; Working Group on the Probabilities of Future Large Earthquakes in Southern California 1992) considered Coulomb stress changes, but only for the permanent effect associated with the most recent large earthquake in the region. In contrast, we find that the transient effect dominates during the first decade after the triggering event, contributing both to the production of aftershocks and to the higher likelihood of subsequent main shocks. This result may help to explain a stress-triggering paradox in southern California: for small-to-moderate southern California earthquakes since 1932, the influence of Coulomb stress changes were discernible for  $< 5$  yr (Harris *et al.* 1995), but persisted for 50 yr following the great 1857  $M = 7.8$  earthquake in the same region (Harris & Simpson 1996). The transient effect decays within 5–10 yr for large and small shocks alike, but only large shocks substantially perturb the permanent probabilities, and so their influence persists long after the transient effect subsides.

Clustering of strong shocks is the outstanding feature of seismicity over historical (Kagan & Jackson 1991) and palaeoseismic (Wallace 1987) time periods. Clustering implies that the prospect of a large earthquake rises after a large event. Stress transfer offers a physical explanation for earthquake clustering and migration: stress drops on the slipped fault but rises at other sites nearby, bringing faults in these regions closer to failure. Coulomb stress calculations thus capture the most salient feature of earthquake distributions, and give insight as to where the next event is more likely to strike.

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